

The Adjoint of CMAQ

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An adjoint model for the internationally used Community Multiscale Air Quality (CMAQ) modeling platform of the U.S. EPA is developed. The adjoint version for CMAQ (CMAQ-ADJ) provides the user community with forward (decoupled direct method or DDM) and backward (adjoint) sensitivity analysis capabilities. Current implementation is for gas-phase processes. Discrete adjoints are implemented for all processes with the exception of horizontal advection, for which, because of inherent discontinuities in the advection scheme, the continuous approach is superior. The adjoint of chemistry is constructed by interfacing CMAQ with the kinetic pre-processor, which provides for increased flexibility in the choice of chemical solver and facilitates the implementation of new chemical mechanisms. The adjoint implementation is evaluated both on a process-by-process basis and for the full model. In general, adjoint results show good agreement with brute-force and DDM sensitivities. As expected for a continuous adjoint implementation in a nonlinear scheme, the agreement is not perfect for horizontal transport. Sensitivities of various air quality, public health, and environmental metrics with respect to emissions are calculated using the adjoint method. In order to show applicability to regional climate studies, as an example, the sensitivities of these metrics with respect to local temperatures are calculated.

Introduction

Three-dimensional (3-D) atmospheric chemical transport models (CTMs) are used to predict spatial and temporal distributions of airborne pollutants. In recent years, they have been increasingly modified to provide information, not only about concentrations, but also sensitivities of atmospheric levels with respect to various parameters. Owing in part to increased computational resources, sensitivity analysis

has received more attention and new methods have been developed to more efficiently calculate sensitivity coefficients (derivatives) of model outputs with respect to various inputs. Sensitivity information provided by atmospheric models can be used in various applications such as the design of optimal pollution-control strategies, inverse modeling and model parameter estimation, and air quality forecasting and data assimilation.

Local sensitivity analysis techniques can be divided into two general categories of forward and backward methods. In the often-used forward method, sensitivities are propagated forward (along the model trajectories) from the perturbed source into various receptors/outputs (1–3). By nature, the methods in this category are efficient in simultaneously providing sensitivity information about all receptors with respect to a few specific parameters (4–7). In backward (adjoint) sensitivity analysis, the perturbation is made at the receptor end and is propagated backward in time and space through an auxiliary set of equations. As a result, adjoint sensitivity analysis provides simultaneous sensitivity information about specific receptors with respect to all sources and parameters.

Adjoint sensitivity analysis in its current form can be traced back to the early stages of nuclear reactor physics in 1940s and 1950s (comprehensive views on the history of the adjoint method for sensitivity analysis are given in 8, 9). Adjoint sensitivity analysis was later applied to various environmental problems (10–15). In particular, it has been used extensively in meteorology and oceanography for various applications such as sensitivity analysis (16, 17), variational data assimilation (18–20), parameter estimation (21), etc. In the past decade, adjoint analysis has been extended to 3-D CTMs. Elbern et al. (22–25) developed an adjoint for the EURAD CTM and performed chemical data assimilation and inverse modeling of emissions. Vukicevic and Hess (26) implemented the adjoint method in the tracer model HANK and performed sensitivity analysis with respect to various parameters. More recently, adjoint versions for other global or regional CTMs have been developed for various applications such as inverse modeling and sensitivity analysis; these include regional models CHIMERE (27–29), STEM (30–32), Polair (33–34), CIT (35, 36), and DRAIS (37) and global models IMAGES (38, 39), TM4 (40), and GEOS-Chem (41). However, among the regional and air quality models for which an adjoint version is available, none is widely used in the modeling community. In this work, we develop an adjoint for the Community Multiscale Air Quality (CMAQ) model of the U.S. EPA (42, 43). CMAQ is generally considered as the most widely used regional air quality model in the U.S. and across the world. Furthermore, we demonstrate how the adjoint model can be used for sensitivity analysis of various air quality and/or environmental metrics. The adjoint method, in tandem with the decoupled direct method (DDM), provides the users of CMAQ with a powerful set of analysis tools that can tackle a wide spectrum of problems.

Development of the Adjoint. Atmospheric CTMs are based on the atmospheric diffusion equation (44, 45)

$$\frac{\partial C_i}{\partial t} = -\mathbf{u} \cdot \nabla C_i + \frac{1}{\rho} \nabla \cdot (\rho \mathbf{K} \nabla C_i) + R_i + E_i \quad (1)$$

where C_i is the mixing ratio of species i (a function of 3-D space and time), \mathbf{u} is the vector wind field, \mathbf{K} is the diffusivity tensor, E_i represents elevated emissions, ρ is the air density, and R_i is the net chemical reaction rate for the species. Equation 1 is solved subject to specified initial and boundary conditions. In operator notation, the model operator matrix,

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\mathbf{M} , maps the input parameters vector α (including initial conditions) into the output domain

$$\mathbf{C} = \mathbf{M}\alpha \quad (2)$$

where \mathbf{C} is the concentration vector at the end of the integration period (t_F). For most common applications, principal input parameters are initial and boundary concentrations and emission rates, but they may also include other parameters such as chemical reaction rate constants, dry deposition velocities, etc. Equation 1 and the operator \mathbf{M} can be referred to as the *forward model* and operator, respectively. Note that owing to nonlinearity in gas-phase chemistry, \mathbf{M} is a nonlinear operator. Transport processes (horizontal and vertical advection and diffusion) in eq 1, on the other hand, are physically linear processes, although these terms may be integrated numerically by nonlinear schemes in the discretized form.

A perturbation in the input parameters (e.g., emissions δE_i) in eq 1 results in a perturbation in each predicted concentration, δC_i , which is governed by

$$\frac{\partial \delta C_i}{\partial t} = -\mathbf{u} \cdot \nabla (\delta C_i) + \frac{1}{\rho} \nabla \cdot (\rho \mathbf{K} \nabla \delta C_i) + \mathbf{F}_i \delta \mathbf{C} + \delta E_i \quad (3)$$

where \mathbf{F}_i is the i th row of the Jacobian of the chemical reaction rates ($F_{ij} = \partial R_i / \partial C_j$). Equation 3 can be represented in operator form as

$$\delta \mathbf{C} = \mathbf{L} \delta \alpha \quad (4)$$

where \mathbf{L} is the Jacobian of the model operator at the base case conditions. Equations 3 and 4 represent the linearized form of the forward model/operator, and are referred to as the tangent linear model (TLM) and operators, respectively. Note that eq 3 is also equivalent to the system of sensitivity equations solved in the DDM (2, 3) for sensitivity analysis; TLM and DDM can be used interchangeably to refer to the forward method for calculation of first-order local (in the sense of a small perturbation) sensitivity coefficients, e.g., $\delta C_i / \delta E_j$.

If one defines a scalar cost function of the concentration field computed by the model (forms of the cost function for problems of interest in the application of CMAQ are discussed in Section 4) as

$$J = \int_t \int_\omega g(\mathbf{C}, t, \omega) \, d\omega \, dt \quad (5)$$

where ω is the generalized spatial coordinate, then an *adjoint model* to the TLM/DDM can be derived by applying Lagrange multipliers and integration by parts to eq 3 and its associated initial and boundary conditions

$$-\frac{\partial \lambda_i}{\partial t} = \nabla \cdot (\mathbf{u} \lambda_i) + \nabla \cdot \left(\rho \mathbf{K} \nabla \frac{\lambda_i}{\rho} \right) + \mathbf{F}_i^T \lambda + \varphi_i \quad (6)$$

where \mathbf{F}_i^T is the i th row of the transposed Jacobian (or the transpose of the i th column of the original Jacobian) of the chemical reaction rates, λ_i is the adjoint variable for species i such that at each time and location $\lambda_i = \partial J / \partial C_i$, and φ_i is the forcing term for the adjoint equations

$$\varphi_i = \frac{\partial g}{\partial C_i} \quad (7)$$

Details of the derivation of adjoint equations and related initial and boundary conditions for a CTM can be found in Elbern et al., 2000 (24), Sandu et al. 2005 (30), Hakimi et al., 2005 (31), Martien et al., 2006 (35), and Henze et al., 2007 (41). Equation 6 is challenging to solve owing to the

TABLE 1. Comparison of Computational Times for the Forward, DDM, and Adjoint Models with Various Chemical Solvers at the Default/Recommended Settings

solver ^a	normalized computational times ^b		
	forward model ^c	DDM ^{d,e}	adjoint ^d
CMAQ-EBI	1.00		
CMAQ-ROS3	2.10		
CMAQ-SMVGear	3.69		
KPP-ROS2	1.59	1.88	2.02
KPP-ROS3	1.08	1.96	2.02
KPP-ROS4	1.18	2.11	2.11
KPP-RODAS3	0.96	2.12	2.09
KPP-RODAS4	1.18	2.39	2.18
KPP-RADAU-2A	2.08	7.81	7.87
KPP-LOBATTO	2.66	7.93	7.25
KPP-GAUSS	2.66	8.13	5.41
KPP-RADAU-1A	1.99	7.60	7.96

^a For description of solvers, see refs 55–58. ^b All simulations are carried out sequentially for 24 hours, on 64 bit, 2.0 GHz dual-core Opteron processors. ^c Values are normalized to forward simulation with EBI solver. ^d Values are normalized to the forward simulation with the same solver. ^e Values include the time required for concentration integrations.

concentration-dependent cost function and the associated forcing term, φ_i . The negative sign preceding the transient term in eq 6 indicates that the adjoint equations are integrated backward in time. Calculation of the Jacobian of the reaction rates in eqs 3 and 6 requires values of the state vector (concentrations). For TLM/DDM calculations, this is achieved easily, as the integrations for the TLM/DDM and forward models may be advanced together. For adjoint calculations, however, concentrations need to be stored (so-called *checkpointed*) in forward simulations and then used for backward integration. Checkpointing is also necessary for any other nonlinear process that is simulated in the backward mode.

The TLM/DDM equations are driven/forced by perturbations in the inputs/sources (e.g., ϵE in eq 3). These perturbations are then propagated forward in time to produce a field of sensitivity coefficients with respect to the perturbed input/source parameter. On the other hand, the forcing terms for the adjoint equations are perturbations in a scalar, receptor-based cost function (i.e., φ_i in eq 6) that are propagated backward in time. Therefore, integration of the adjoint equations results in a field of sensitivity coefficients of the cost function with respect to model inputs. TLM/DDM is a source-based forward sensitivity method suitable for calculating sensitivities of a large number of outputs with respect to a few inputs. Adjoint sensitivity analysis, on the other hand, is a receptor-based, backward method that is most efficient in calculating the sensitivities of a few outputs with respect to numerous inputs. The duality in the range of efficiency and applicability for forward (TLM/DDM) and backward (adjoint) sensitivity analysis methods makes them complementary approaches for addressing a wide spectrum of problems.

The adjoint of a linear operator \mathbf{L} can also be defined using the following duality principle

$$\langle \mathbf{u}, \mathbf{L}\mathbf{v} \rangle_n = \langle \mathbf{L}^* \mathbf{u}, \mathbf{v} \rangle_n \quad (8)$$

where \mathbf{L}^* is the adjoint operator and $\langle \cdot, \cdot \rangle_n$ denotes the inner product in R^n . Applying eq 8 to the TLM/DDM model,

$$\langle \delta \mathbf{C}, \mathbf{L} \delta \alpha \rangle = \langle \mathbf{L}^* \delta \mathbf{C}, \delta \alpha \rangle \quad (9)$$

Or

$$(\mathbf{L} \delta \alpha)^T (\mathbf{L} \delta \alpha) = \delta \alpha^T \mathbf{L}^* (\mathbf{L} \delta \alpha) \quad (10)$$

which can be used for verification of the adjoint operator from a validated TLM/DDM model (46).

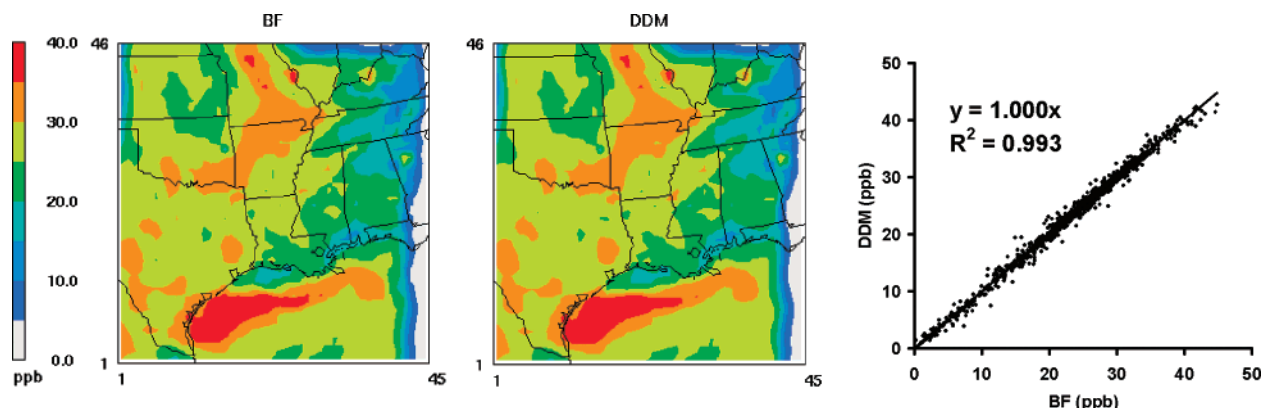


FIGURE 1. Comparison between BF (left) and DDM (middle) seminormalized sensitivities of ozone with respect to initial ozone concentration after 6 h of simulation. BF sensitivities are central difference approximations unless otherwise specified.

Two approaches exist for integration of the adjoint equations. In the continuous approach, the adjoint eqs 6 are discretized and solved numerically. Alternatively, discrete adjoint models may be developed directly from the discretized DDM model. The two approaches in general produce different results, as adjoint and discretization operations are not commutable (47). Note that the same distinction can be made between continuous and discrete approaches for the development of TLM/DDM models.

In eqs 2 and 4, it is assumed that the evolution of concentrations or sensitivities is described by a single operator. In practice, CTMs use an operator splitting scheme, and they also integrate the governing equations over multiple time steps. The overall operator can be considered as the composition of all internal steps. In other words, for a model of N time steps and m processes at each step,

$$M = (M_{p_1}^1 \circ M_{p_2}^1 \circ \dots \circ M_{p_m}^1) \circ \dots \circ (M_{p_1}^N \circ M_{p_2}^N \circ \dots \circ M_{p_m}^N) \quad (11a)$$

$$L = (L_{p_1}^1 \circ L_{p_2}^1 \circ \dots \circ L_{p_m}^1) \circ \dots \circ (L_{p_1}^N \circ L_{p_2}^N \circ \dots \circ L_{p_m}^N) \quad (11b)$$

$$L^* = (L_{p_m}^N)^T \circ (L_{p_{m-1}}^N)^T \circ \dots \circ (L_{p_1}^N)^T \circ \dots \circ (L_{p_m}^1)^T \circ (L_{p_{m-1}}^1)^T \circ \dots \circ (L_{p_1}^1)^T \quad (11c)$$

Implementation of the Adjoint (CMAQ-ADJ)

In this work, adjoint (and DDM) methods are implemented in CMAQ version 4.5.1 for gas-phase processes. (For identification purposes, this code is referred to as CMAQ-ADJ.) As there are no significant changes in these processes in the recently released version 4.6, the adjoint model implementation can be equally applied to CMAQ 4.6. We use a hybrid approach in development of the adjoint (and DDM) model(s), wherein discrete adjoints for chemistry, diffusion, and vertical advection and continuous adjoints for horizontal advection are employed. As explained later, these choices are made based on accuracy of the adjoints as well as their physical significance.

A variation of DDM (4, 7) has been previously implemented in CMAQ (48). Implementation of DDM is briefly addressed to complement the discussion of adjoint implementation. The previous implementation of DDM in CMAQ employed a continuous approach. In the present DDM implementation, a discrete approach for chemistry integration is used to enhance accuracy (see discussion on the chemistry adjoint below). Complete validation of the DDM results is not shown here, but in general they are in good agreement with brute-force (BF) finite difference calculations (Figure 1). Note that minor disagreements between DDM and BF results in Figure 1 are primarily a result of the use of a continuous approach for calculating DDM sensitivities

of horizontal advection. The use of a discrete approach for horizontal advection will enhance agreement between BF and DDM but may produce physically inconsistent results (see discussion on horizontal advection below). The same problem will occur in vertical advection for earlier versions of CMAQ where a nonlinear scheme was employed.

The validation of DDM results with BF sensitivities is a rather straightforward task, as they both provide forward sensitivity fields. Validation of adjoint results cannot be achieved as easily. For each pair of forward (DDM or BF) and backward (adjoint) sensitivity simulations, there is only one point-of-comparison available for validation purposes. Depending on the definition of the forward sensitivity parameter (perturbed source) and adjoint cost function (perturbed receptor), the point-of-comparison can be the sensitivity of a single output or an integrated concentration metric to changes in a single input or collective change to a set of inputs. Regardless of the source and receptor metrics involved, available points-of-comparison between each pair of forward and backward sensitivity fields is reduced to a single scalar. Therefore, a complete validation of adjoint variables for all locations, times, and species is pragmatically infeasible. In the following sections, we describe the methods used for the implementation of adjoint analysis in CMAQ and then for validation purposes we will introduce reduced models where points-of-comparison between forward and backward sensitivity fields are increased. For example, for chemistry validation, forward and backward simulations are carried out only for chemistry (transport processes turned off). Therefore, the 3-D model can be considered as an ensemble of numerous box models, each of which provides a point-of-comparison. The reduced chemistry-only model will then provide a 3-D (in space only) field of points-of-comparison between forward and backward sensitivity fields.

Chemistry Adjoint. In order to implement forward and backward sensitivity analysis capabilities, the *Kinetic Pre-Processor* (KPP), version 2.2 (49, 50), has been integrated into CMAQ. KPP can be efficiently used to generate required subroutines for any chemical mechanism. Recent versions of KPP have been extended to include DDM and adjoint sensitivity analysis capabilities (51–53). KPP significantly enhances the flexibility of CMAQ for using new or modified chemical mechanisms. Chemical solvers offered in KPP are generic and independent of mechanism, and therefore, migration to a new chemistry can be achieved seamlessly. The latest version of KPP offers a choice from multiple Rosenbrock (54, 55) and Runge–Kutta solvers (including families of fully implicit three-stage and singly diagonally implicit Runge–Kutta methods, see 56), where within each family various solvers differ in accuracy and stability properties. KPP generates all required subroutines for continuous

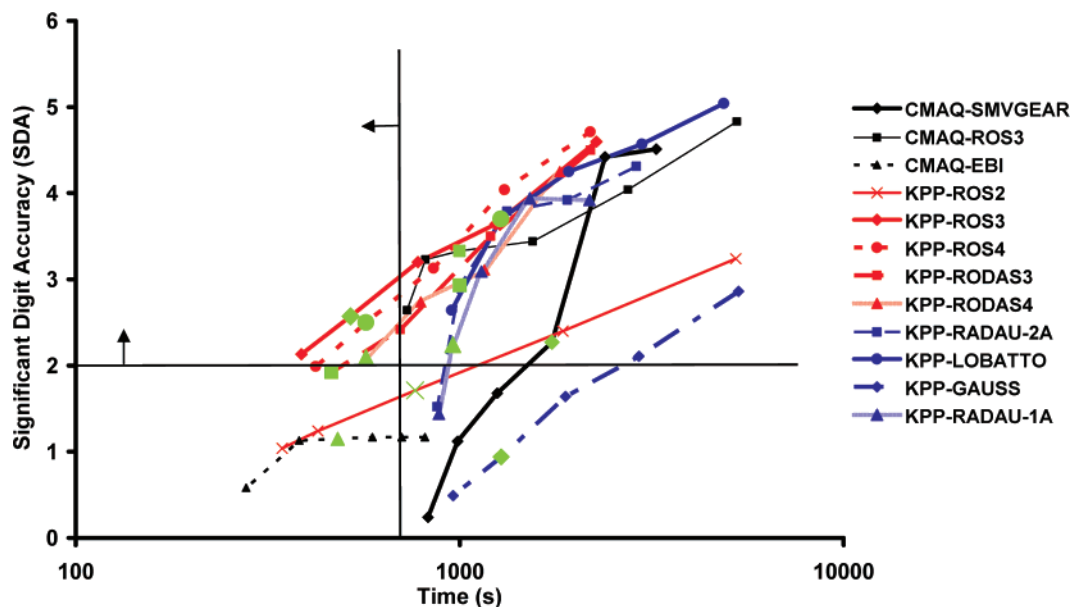


FIGURE 2. Work–precision diagrams for day-long simulations with various CMAQ (black) and KPP solvers (Rosenbrock in red and Runge–Kutta in blue). Significant digit accuracy (SDA) for each species is defined as $SDA_i = -\log(RMSRE_i)$, where RMSRE is the root-mean square of relative error in comparison with a reference solution. Diagrams are shown for the overall SDA (minimum across all species). Simulations with default/recommended settings are indicated by enlarged, green markers. For this application, most Rosenbrock solvers fall in the desirable performance region.

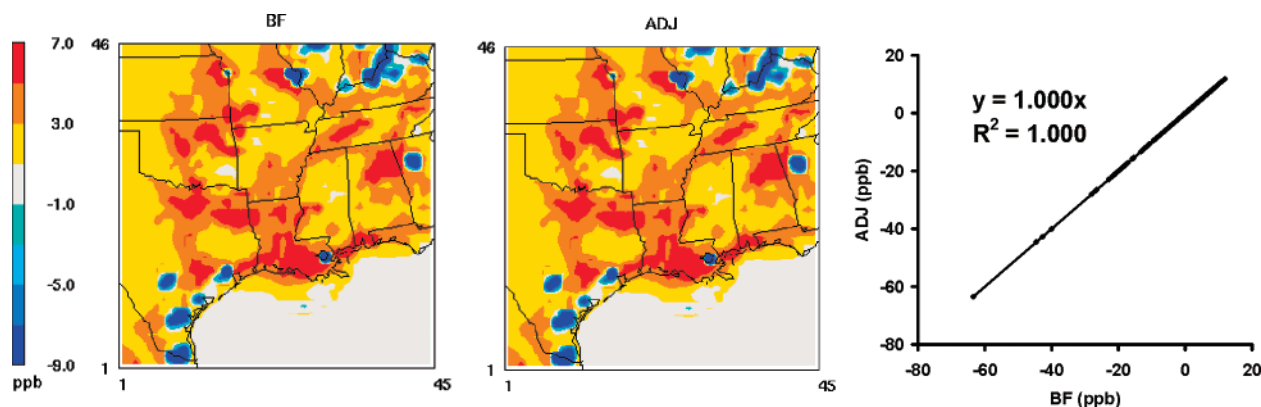


FIGURE 3. Comparison of adjoint and BF sensitivities of final ozone concentration with respect to initial NO concentration; chemistry-only simulations are carried out for 6 h.

and discrete DDM and adjoint sensitivity calculations. In general, KPP solvers compare favorably with CMAQ's SMVGEAR (57), ROS3, and Euler backward iterative (EBI) (58) solvers. At the default tolerance values, CPU time requirement for KPP's Rosenbrock solvers are comparable with EBI and lower than CMAQ's SMVGEAR and ROS3 (Table 1) solvers. Work–precision diagrams (55) for model simulations with original CMAQ solvers as well as those of KPP are shown in Figure 2. These diagrams suggest that KPP's Rosenbrock solvers provide fairly accurate solutions at relatively low computational cost and outperform original CMAQ solvers.

State vectors (concentrations) are checkpointed at synchronization (chemistry) time steps into netCDF files. Currently, checkpointing is available only for fixed time steps in each simulation day. Therefore, predetermined synchronization steps are set for each day. Checkpoints are written during the forward simulations. During the backward simulations, checkpointed concentrations are read at the beginning of each synchronization time step. The required checkpoints at the internal chemistry time steps are recalculated by forward integration of the concentrations for the synchronization time step (i.e., two-level checkpointing, see 30, 59). Calculated chemistry-only adjoint sensitivities are in close agreement with BF values (Figure 3).

Horizontal Advection Adjoint. CMAQ version 4.5 uses the piecewise parabolic method (60) to integrate the flux form of the one-dimensional horizontal advection equation

$$\frac{\partial(\eta)}{\partial t} = -\frac{\partial(u\eta)}{\partial x} \quad (12)$$

where η is the mass-based concentration vector ($\eta = \rho C$, where ρ is air density). If total mass continuity holds for the advection process, then eq 12 is equivalent to

$$\frac{\partial C}{\partial t} = -u \frac{\partial C}{\partial x} \quad (13)$$

The application of a mass-based adjoint variable (for conservation) to eq 13 results in the following one-dimensional adjoint advection equation

$$-\frac{\partial(\lambda_m)}{\partial t} = \frac{\partial(u\lambda_m)}{\partial x} \quad (14)$$

where λ and λ_m are mixing ratio and mass-based adjoint variables ($\lambda_m = \lambda/\rho$). Therefore, the one-dimensional adjoint

TABLE 2. Forward and Backward Simulation Schemes in CMAQ

Forward Model	Adjoint Model
INIT (t=0)	INIT (t=tF)
DO (Synchronization steps)	DO (Synchronization steps)
DO (Advection steps)	DO (Advection steps)
V-DIFF	FORCE-ADJ
COUPLE	NEXTIME (-TSTEP)
H-ADV	READ CHECKPOINT (CONC)
WRITE CHECKPOINT (Density)	CHEM-ADJ
V-ADV	H-DIFF-ADJ
H-DIFF	READ CHECKPOINT (Density)
DECOUPLE	DECOUPLE
WRITE CHECKPOINT (CONC)	V-ADV-ADJ
CHEM	H-ADV-ADJ
NEXTIME (TSTEP)	COUPLE
END DO	V-DIFF-ADJ
WRITE CONC	END DO
END DO	WRITE ADJ
	END DO

advection equations solved in the continuous adjoint implementation are

$$-\frac{\partial(\lambda/\rho)}{\partial t} = \frac{\partial(u\lambda/\rho)}{\partial x} \quad (15)$$

where all Dirichlet boundary conditions for the adjoints are set to zero. In forward simulations, mixing ratios are “coupled” with (multiplied by) densities (i.e., they are converted to mass-based concentrations) for advection processes. Subsequently, after the completion of each advection step, mass-based concentrations are “decoupled” from (divided by) densities and converted back to mixing ratios. Unlike the forward calculations, in the backward simulation, the conversion of mixing ratio to mass-based adjoints is accomplished by division by densities (see Table 2 for an operational scheme of the forward and backward simulations).

Figure 4 shows comparisons between adjoint and BF horizontal advection sensitivities. The simulations for Figure 4 include only horizontal advection in the x direction, where the figure shows an x cross section (for 23 vertical layers) of sensitivities of ozone at the final time step in the 20th column of the domain with respect to initial ozone concentrations in the 20th column. By considering advection in the x direction as the sole process, a two-dimensional field of point-of-comparison between forward and backward sensitivity fields is available for visualization. BF sensitivities are calculated by various changes to the initial ozone at the 20th column. As can be seen, the general features of the advected fields are similar, but there are noticeable differences between the forward and backward fields. The adjoint field is smoother while negative sensitivities in the BF field are physically meaningless; negative sensitivities represent only numerical noise in the BF fields. The behavior seen in Figure 4 is consistent with previous studies of the adjoints of nonlinear advection schemes (41, 61, 62). Also note that BF fields are inconsistent among themselves (for various perturbations) and deviate further from the backward field for smaller perturbations. This indicates that differences between BF and adjoint fields are not a result of nonlinearities in the advection scheme, as they increase with decreasing perturbations. These differences instead result from discontinuity and nondifferentiability in the forward scheme that causes irrecoverable inconsistencies between BF simulations (63). If a discrete adjoint approach is employed in these simulations, the resulting adjoint field would resemble a noisy BF sensitivity field. As a result of these inconsistencies, we conclude that for the current nonlinear advection scheme in CMAQ, continuous adjoint implementation of the horizontal advection scheme is superior to discrete implementation.

Vertical Advection Adjoint. CMAQ uses an upwind first-order finite difference scheme for solving the vertical

advection equation

$$\frac{\partial(\eta)}{\partial t} = -\frac{\partial(w\eta)}{\partial z} \quad (16)$$

In CMAQ version 4.5, vertical advection is used as a mass conservation step. During horizontal advection, air densities are also advected alongside concentrations. In each ensuing vertical advection step, the vertical wind profile is calculated such that transported air density for that time step at each level matches meteorological densities from MM5. The calculated vertical wind profile is then applied to all species. It is necessary to use a vertical wind profile during backward calculations similar to that used in the forward simulations. Therefore, either transported air densities after each horizontal advection step or the calculated vertical wind profile at each vertical advection step during forward simulations need to be checkpointed.

Similar to horizontal advection, the corresponding adjoint equation for vertical advection is

$$-\frac{\partial(\lambda/\rho)}{\partial t} = \frac{\partial(w\lambda/\rho)}{\partial z} \quad (17)$$

The same numerical subroutine may be used with the reverse vertical wind profile (continuous adjoint). In our implementation, a discrete adjoint is developed for the linear scheme used in vertical advection. Applying the adjoint (transpose) of the linear operator above (discrete adjoint) yields different results than using the forward operator with the reverse wind profile (continuous adjoint). The discrete adjoint provides results that are more consistent with BF sensitivities (Figure 5). Note that in previous versions of CMAQ (before version 4.5) where a nonlinear scheme is used for vertical advection, a continuous approach would be preferable.

Vertical Diffusion Adjoint. CMAQ provides an option for species emissions to be processed during chemistry or vertical diffusion integrations. In the present adjoint implementation, emissions are injected during vertical diffusion for which the following equation

$$\frac{\partial C}{\partial t} = \frac{\partial}{\partial z} \left(K \frac{\partial C}{\partial z} \right) \quad (18)$$

is solved with the corresponding adjoint equation as

$$-\frac{\partial \lambda}{\partial t} = \frac{\partial}{\partial z} \left(K \frac{\partial \lambda}{\partial z} \right) \quad (19)$$

Deposition velocities are included in the first layer as part of the boundary conditions. The same numerical scheme can be used for adjoint integrations by excluding only the emissions. Equation 20 is evolved to the next time step by applying the following operator

$$C^{n+1} + (\text{LHS})^{-1}[(\text{RHS})C^n + E^n] \quad (20)$$

where LHS and RHS are tridiagonal left-hand side and right-hand side matrices in a Crank–Nicholson discretization, respectively. Therefore, the discrete adjoint operator is

$$\lambda^n = (\text{RHS})^T (\text{LHS})^{-T} \lambda^{n+1} \quad (21)$$

For vertical diffusion, discrete and continuous adjoints produce nearly identical results. We use the continuous

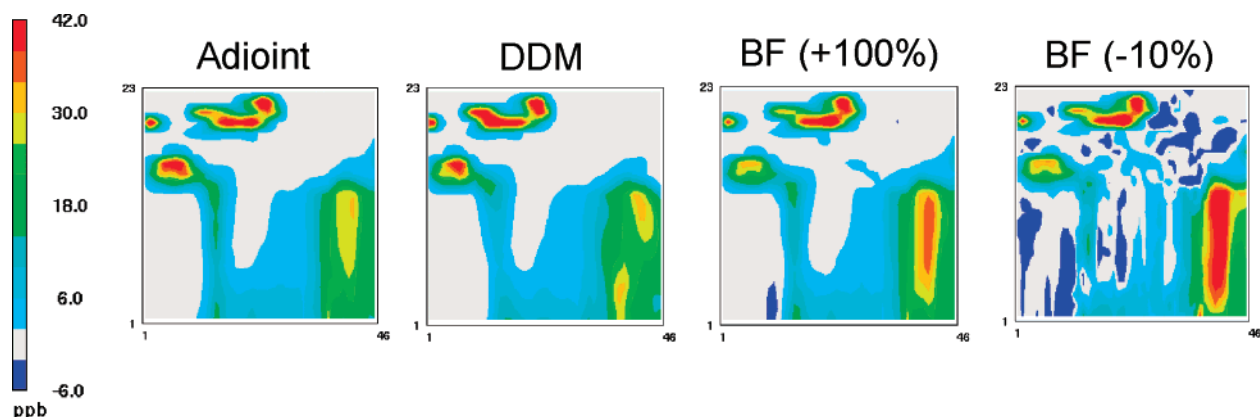


FIGURE 4. Comparison of various BF with the adjoint sensitivity of ozone at the 20th column with respect to initial ozone at the 20th column. Only horizontal advection in the x direction is included in the simulations. The DDM sensitivity shows reasonable agreement with that of the adjoint.

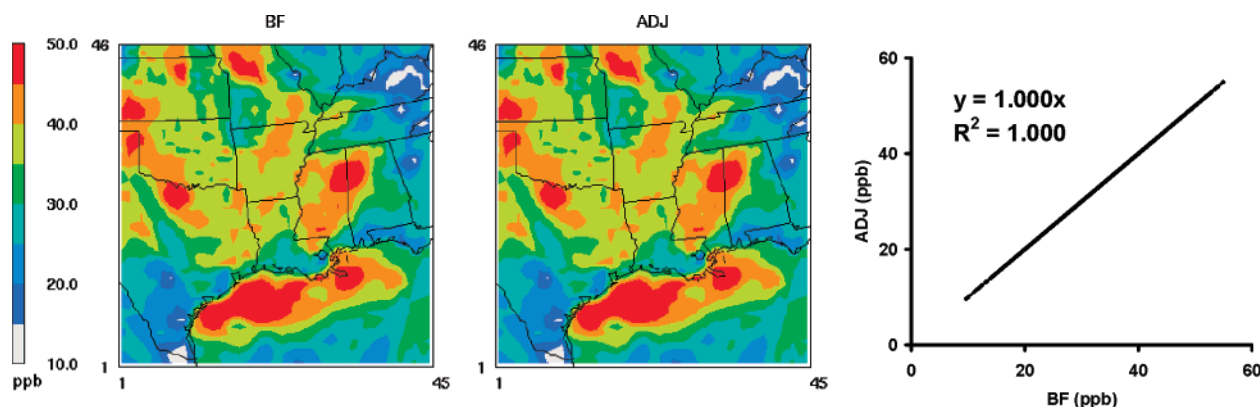


FIGURE 5. Simulations with only vertical advection for calculation of the sensitivities of surface ozone with respect to the initial surface ozone.

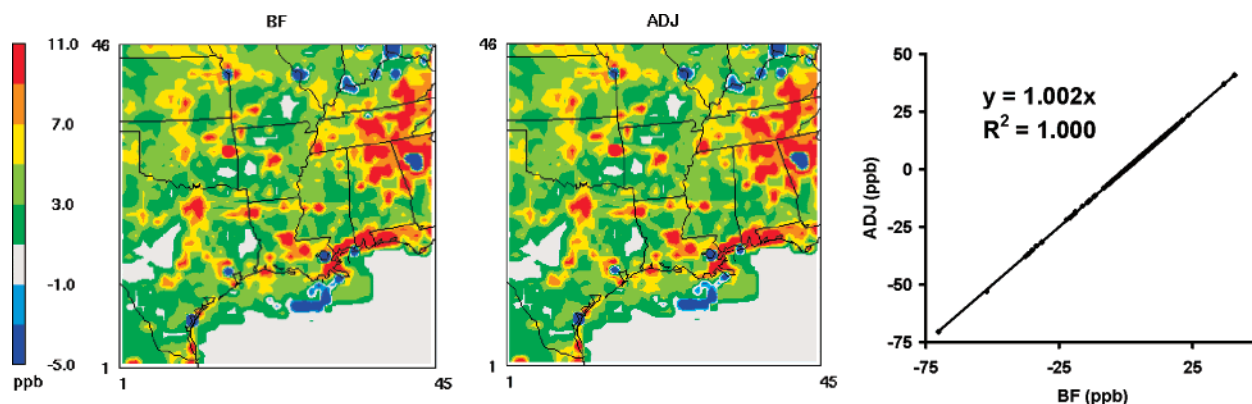


FIGURE 6. Simulations with only chemistry and vertical diffusion; normalized sensitivities of surface ozone with respect to the surface emissions of NO.

approach in the present implementation. The gradients of the cost function with respect to emissions can be calculated from the adjoint variables during backward integrations:

$$\frac{\partial J}{\partial E^n} = \left(\frac{\partial C^{n+1}}{\partial E^n} \right)^T \left(\frac{\partial J}{\partial C^{n+1}} \right) = (\text{LHS})^{-1} \lambda^{n+1} \quad (22)$$

Note that the required factorization in eq 23 is already carried out for continuous adjoint integration. Therefore, calculation of the gradient of the cost function with respect to emissions of each species is accomplished by the minimal cost of one additional back-substitution in the modified tridiagonal solver used in the adjoint integration.

Figure 6 compares BF and adjoint sensitivity fields for sensitivities of ozone at the surface with respect to surface NO emissions when simulations include only chemistry and vertical diffusion. As the accuracy of chemistry adjoints has been previously verified, the agreement shown in Figure 6 serves as validation of both the adjoint of vertical diffusion and calculation of emission gradients.

Horizontal Diffusion Adjoint. In CMAQ, species undergo horizontal diffusion according to the following equation

$$\frac{\partial C}{\partial t} = \frac{1}{\rho} \frac{\partial}{\partial x} \left(\rho K \frac{\partial C}{\partial x} \right) \quad (23)$$

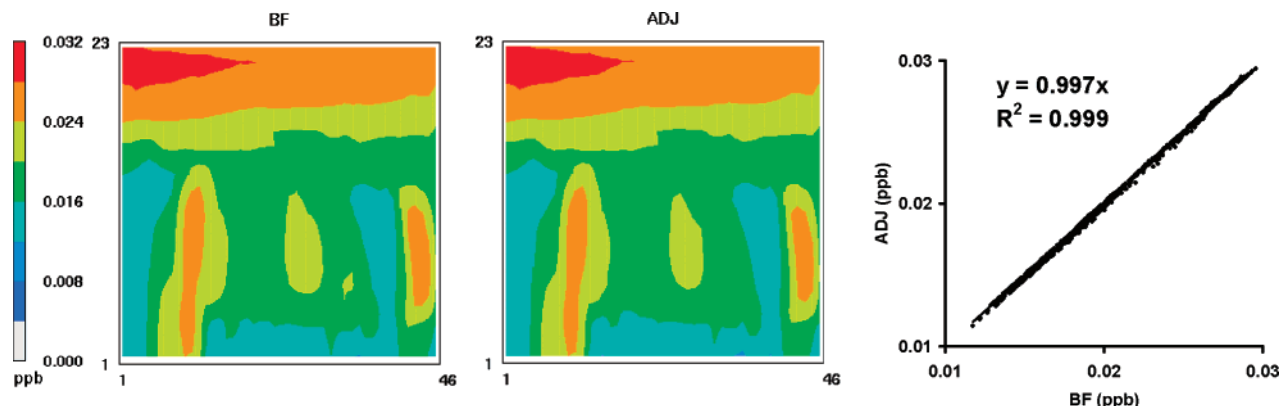


FIGURE 7. Simulations with only horizontal diffusion in the x direction for the calculation of ozone sensitivities at the 21st column with respect to initial ozone at the 20th column.

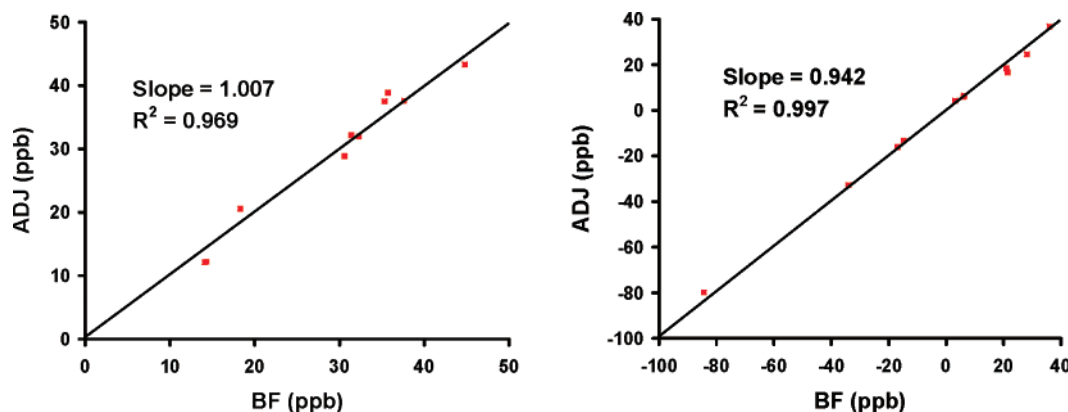


FIGURE 8. Full model simulations; sensitivities of surface ozone with respect to surface NO initial concentrations (left) and emissions (right) for selected locations. Values are shown in comparison to the one-on-one lines.

the continuous adjoint of which is

$$-\frac{\partial \lambda}{\partial t} = \frac{\partial}{\partial x} \left(\rho K \frac{\partial (\lambda / \rho)}{\partial x} \right) \quad (24)$$

The horizontal diffusion operator is symmetrical and, therefore, self-adjoint. As a result, (a) the same numerical scheme can be used to horizontally diffuse concentrations and adjoints in forward and backward simulations, and (b) continuous and discrete horizontal diffusion adjoints are identical. We use the same subroutine for horizontal diffusion of adjoints with an internal “decoupling” from (division by) densities (see Table 2). Adjoint and BF sensitivity fields show good agreement in Figure 7 where only horizontal diffusion in one direction is included in the simulations and sensitivities of final ozone at the 21st x cross section with respect to initial ozone at the 20th column are shown.

Overall Implementation. In the present implementation, forward and backward (and DDM) models are run as separate, independent models. For executing adjoint and DDM models, one first needs to once carry out the forward simulation and store the generated checkpoint files. For subsequent adjoint (and DDM) simulations, however, execution of the forward model is not required, as the same checkpoint files can be re-used. This leads to significant computational savings when multiple backward simulations are performed. In general, the order in which processes are called during the backward simulation is reverse of that in the forward simulation (Table 2). As only chemistry requires knowledge of concentrations in the current implementation, checkpoints are written and read before each chemistry call. However, transported air densities are written to checkpoint files after each horizontal advection scheme in the forward mode and read before each vertical advection scheme in the backward simulation.

In summary, validation of full adjoint results (including all processes) with forward sensitivity fields (BF or DDM) is possible only for a few sensitivity coefficients. Validation of the adjoint of isolated processes through comparison with forward sensitivity fields can be carried out for a larger number of points-of-comparison (Figures 3–7) and provides for a more robust verification procedure. Full model results are also in good agreement with BF sensitivities as shown in Figure 8 for few select points and types of sensitivity coefficients.

Computational Efficiency. The original CMAQ provides three options for chemical solvers in Euler backward iterative (EBI), a vectorized Gear solver (SMVGEAR), and ROS3 from the family of Rosenbrock solvers. With the implementation of KPP, users of CMAQ-ADJ have access to five Rosenbrock and four Runge–Kutta solvers that differ in the order of integration method. Unlike the original implementation of ROS3 in CMAQ, KPP implementation does not employ cell blocking for improved performance on vectorized machines. Table 1 shows the comparison of computational times for forward, DDM, and adjoint models with various solvers. All tests are carried out for a 1 day simulation for a $45 \times 46 \times 18$ computational domain with 36 km horizontal resolution. In these simulations, the CB-IV chemical mechanism is used. Computational times for forward runs are normalized to the simulation time for the model with CMAQ’s EBI solver. Overall, the EBI solver provides the fast simulation times; however, it has the lowest accuracy. For similar tolerance limits, all other solvers show similar good accuracy. Rosenbrock solvers, however, outperform other groups in these tests that are carried out on nonvectorized machines (Figure 2). Also shown in Table 1 are the relative costs of forward and backward sensitivity calculation. Backward calculations

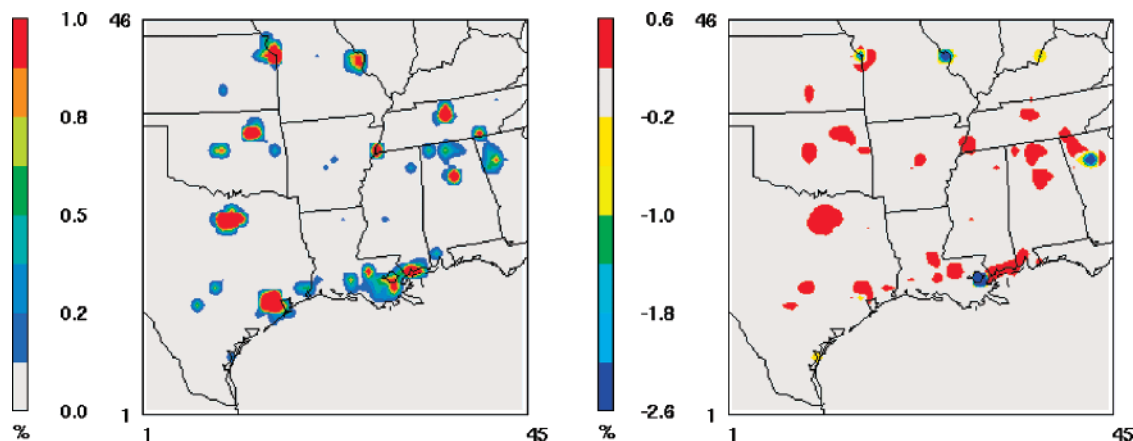


FIGURE 9. Spatial distribution of the cost function for population exposure (left) and associated gradients with respect to NO_x emissions (right). Values are normalized to the total cost function and presented in percent. The exposure threshold is 60 ppb.

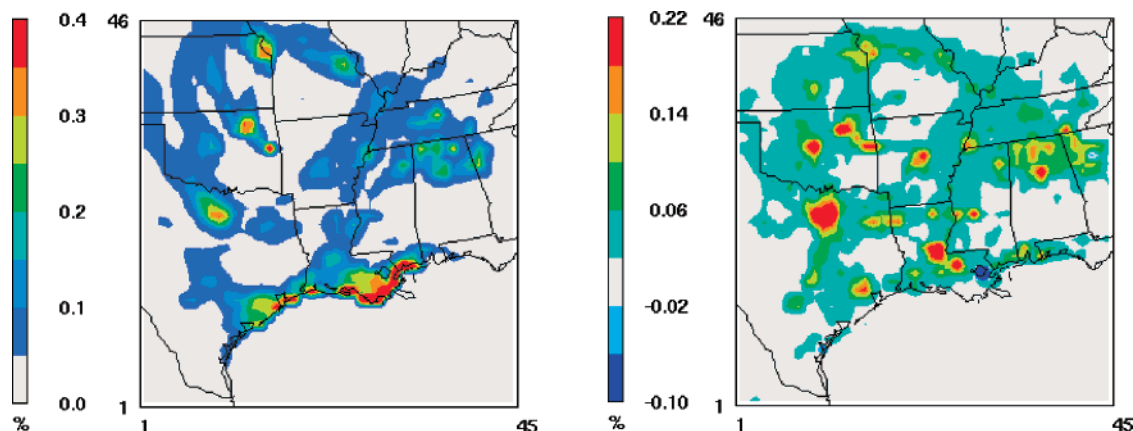


FIGURE 10. Spatial distribution of the cost function for the W-126 metric of vegetation exposure from ozone (left) and associated gradients with respect to NO_x emissions (right). Values are normalized to the total cost function and presented in percent.

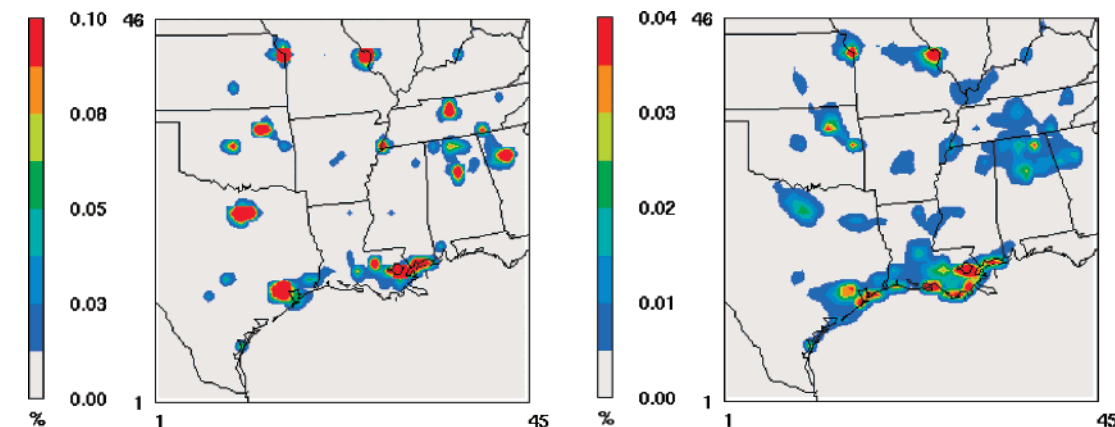


FIGURE 11. Temperature gradients of the population exposure to ozone (left) and the W-126 metric (right) with respect to local temperatures. Values are integrated for the duration of the episode, normalized to the total cost function, and presented in percent.

require at least twice the computational time as forward calculations (significantly more for Runge–Kutta solvers); as in the two-level checkpointing scheme, a second-level forward integration is performed for retrieval of concentrations at the internal time steps in between checkpoint intervals. Finally, note that the relative costs in Table 1 are for a single receptor/cost function (in adjoint mode) or source/sensitivity parameter (in DDM mode). When sensitivities for multiple receptors or sources are calculated simultaneously, the overall cost per receptor/source for both DDM and adjoint simulation is significantly reduced. This is a result of the shared computational cost in matrix factorization among various receptors/sources. The potential

saving is more substantial for large chemical mechanisms where chemistry integration is a larger contributor to the overall computational cost.

Applications in Receptor-Based Sensitivity Analysis

The adjoint method has been used widely for variational data assimilations and inverse modeling. In these applications, the cost function can be defined generally as

$$J = J_{\text{Observations}} + J_{\text{Background}} \\ = \frac{1}{2}(\mathbf{C} - \mathbf{C}_{\text{obs}})^T \mathbf{O}^{-1}(\mathbf{C} - \mathbf{C}_{\text{obs}}) + \frac{1}{2}(\boldsymbol{\alpha} - \boldsymbol{\alpha}^b)^T \mathbf{B}^{-1}(\boldsymbol{\alpha} - \boldsymbol{\alpha}^b) \quad (25)$$

where C_{obs} is a set of observed concentrations, α^b is the vector of *a priori* (background or initial guess) estimate of inputs, and where \mathbf{O} and \mathbf{B} are observation and background error covariance matrices. The cost function consists of two parts: the first part is a measure of model prediction errors, and the second part is a penalty for deviation from *a priori* estimates of model inputs. In typical applications, the adjoint method is used to calculate the gradients of the cost function with respect to initial concentrations (for data assimilation applications) or model parameters such as emissions (for inverse modeling applications). These gradients are then used in an iterative optimization algorithm in order to minimize the cost function, which reduces the mismatch between model predictions and observations by adjusting the inputs (e.g., emissions) within a reasonable range. Variational methods provide an important approach for constraining emissions of various species on a spatially resolved basis (36).

The adjoint method is a powerful tool for receptor-oriented sensitivity analysis. As a receptor-based method, adjoint sensitivity analysis is particularly suitable for addressing policy problems. Hakami et al. (64) used the adjoint of a CTM for ozone nonattainment sensitivity analysis over the continental United States. They demonstrated that the adjoint method is a powerful framework for formal analysis of interstate, trans-boundary, and intercontinental transport of pollution. Similar approach can be taken to analyze local nonattainment. Here, we briefly describe a few other potential applications for adjoint sensitivity analysis at regional scales using the adjoint of CMAQ. These applications differ only in the definition of the cost function.

Population Exposure Analysis. If the cost function is defined as a population exposure metric, then the resulting sensitivities identify the most influential parameters (emissions) affecting population exposure

$$J = \sum_{x,y,t} [P(C_i - \gamma)]_{x,y,t} \quad (26)$$

where γ represents an exposure threshold and P is the population at each location. Note that eq 26 can be extended to include dose–response relationships for one or multiple pollutants to represent public health risks. As a target-based method, adjoint analysis can identify the most influential emission sources that contribute to the overall exposure/risk metric (e.g., Figure 9). As expected, this definition of the cost function emphasizes areas with large population densities.

Environmental Exposure. A cost function similar to that in eq 26 can be used to quantify environmental stress resulting from increased pollution levels. For example, an environmental exposure metric based on the W-126 function can be defined to quantify the impact of increased ozone on crops and vegetation (65, 66),

$$J = \sum_{x,y,t} \left[\frac{C_{O_3}}{1 + 4403 \exp(-126C_{O_3})} \right]_{x,y,t} \quad (27)$$

where C_{O_3} is the ozone mixing ratio in ppm. With the use of the above equation as the cost function in adjoint analysis, corresponding (emission) gradients can be calculated (Figure 10). Areas of significant gradients (right panel) indicate sources where emission control can result in largest reductions in the cost function (left panel). The adjoint method affords users the flexibility to combine environmental and public health metrics in a single cost function for integrated analysis of air pollution effects.

Effect of Temperature Variation on Air Pollution Levels. In a manner similar to that for the calculation of emission

gradients, the sensitivity of the cost function with respect to changes in temperature can be calculated by

$$\frac{\partial J}{\partial T^n} = \left(\frac{\partial C^{n+1}}{\partial T} \right)^T \left(\frac{\partial J}{\partial C^{n+1}} \right) = \left(\frac{\partial k^n}{\partial T} \right)^T \left(\frac{\partial C^{n+1}}{\partial k^n} \right)^T \lambda^{n+1} \quad (28)$$

As written, eq 28 describes only the effect of temperature on the cost function via chemistry. Changes in temperatures will also affect biogenic (and anthropogenic) emissions. The results of applying eq 28 in the adjoint analysis for population and environmental exposures above (eqs 26 and 27) are shown in Figure 11. It is interesting that temperature gradients show significant spatial distributions, something that is possible to capture only in a receptor-oriented method, i.e., adjoint sensitivity analysis. Spatial distributions such as those in Figure 11 can be used in conjunction with results from regional climate studies to formally quantify the impact of future climate conditions on regional air quality. These gradients can also be used to quantify contributions to the uncertainties in future (or current) air quality from uncertainty/variability in regional temperatures.

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